



# **THE SIX SIGMA GREEN BELT PRIMER**

© by Quality Council of Indiana - All rights reserved

**Fourth Edition - September, 2022**

**Quality Council of Indiana  
602 West Paris Avenue  
West Terre Haute, IN 47885  
TEL: 800-431-1585  
TEL: 812-533-4215  
FAX: 812-533-4216  
qci@qualitycouncil.com  
<https://www.qualitycouncil.com>**



## VII. MEASURE - PROBABILITY & STATISTICS

**THERE IS ALWAYS A 100%  
PROBABILITY THAT A PIECE OF TOAST  
WILL LAND BUTTERED SIDE DOWN ON  
NEW CARPET.**

**FROM "MURPHY'S LAWS"**



**VII. MEASURE - PROBABILITY & STATISTICS**  
**PROBABILITY AND STATISTICS / BASIC CONCEPTS**

**III.B.1**

## **Probability and Statistics**

**Probability is described in the following topic areas:**

- **Probability and Statistics**
  - **Basic Probability Concepts**
  - **Central Limit Theorem**
- **Statistical Distributions**



**VII. MEASURE - PROBABILITY & STATISTICS**  
**PROBABILITY AND STATISTICS / BASIC CONCEPTS**

**III.B.1**

## **Basic Statistical Terms**

<b>Continuous Distributions</b>	<b>Distributions containing infinite (variable) data points. Examples: normal, uniform, exponential, and Weibull distributions.</b>
<b>Discrete Distributions</b>	<b>Distributions resulting from countable (attribute) data that has a finite number of values. Examples: binomial, Poisson, and hypergeometric distributions.</b>
<b>Decision Distributions</b>	<b>Distribution used to make decisions and construct confidence intervals. Examples: t, F, and chi-square distributions.</b>
<b>Parameter</b>	<b>The true numeric population value, often unknown, estimated by a statistic.</b>
<b>Population</b>	<b>All possible observations of similar items from which a sample is drawn.</b>
<b>Sample</b>	<b>A randomly selected set of units or items drawn from a population.</b>
<b>Statistic</b>	<b>A numerical data value taken from a sample that may be used to make an inference about a population.</b>



**VII. MEASURE - PROBABILITY & STATISTICS**  
**PROBABILITY AND STATISTICS / BASIC CONCEPTS**

**III.B.1**

## **Drawing Valid Statistical Conclusions**

### **Analytical (Inferential) Studies**

The objective of statistical inference is to draw conclusions about population characteristics based on the information contained in a sample. Statistical inference in a practical situation contains two elements: (1) the inference and (2) a measure of its validity. The steps involved in statistical inference are:

- Define the problem objective precisely
- Decide if it will be evaluated by a one or two tail test
- Formulate a null and an alternate hypothesis
- Select a test distribution and a critical value of the test statistic reflecting the degree of uncertainty that can be tolerated (the alpha,  $\alpha$ , risk)
- Calculate a test statistic from the sample
- Compare the calculated value to the critical value and determine if the null hypothesis is to be rejected. If the null is rejected, the alternate must be accepted.



VII. MEASURE - PROBABILITY & STATISTICS  
PROBABILITY AND STATISTICS / BASIC CONCEPTS

III.B.1

## Drawing Valid Conclusions (Continued)

### Enumeration (Descriptive) Studies

Enumerative data is data that can be counted. Useful tools for tests of hypothesis conducted on enumerative data are the chi-square, binomial and Poisson distributions.

**Enumerative study**      A study in which action will be taken on the universe.

**Analytic study**          A study in which action will be taken on a process to improve performance in the future.

### Descriptive Statistics

Numerical, descriptive measures calculated from a sample are called statistics. When these measures describe a population, they are called parameters.

Measures	Statistics	Parameters
Mean	$\bar{X}$	$\mu$
Standard Deviation	s	$\sigma$



VII. MEASURE - PROBABILITY & STATISTICS  
PROBABILITY AND STATISTICS / BASIC CONCEPTS

III.B.2

## Probability

The probability of any event (E) lies between 0 and 1. The sum of the probabilities of all possible events (E) in a sample space (S) = 1. The ratio of the chances favoring an event to the total number of chances for and against the event. Probability (P) is always a ratio.

$$P = \frac{\text{Chances Favoring}}{\text{Chances Favoring Plus Chances Not Favoring}}$$

## Simple Events

If an experiment is repeated a large number of times, (N), and the event (E) is observed  $n_E$  times, the probability of E is approximately:

$$P(E) \approx \frac{n_E}{N}$$



VII. MEASURE - PROBABILITY & STATISTICS  
PROBABILITY AND STATISTICS / BASIC CONCEPTS

III.B.2

## Compound Events

Compound events are formed by a composition of two or more events. The two most important probability theorems are the additive and multiplicative. For the following discussion,  $E_A = A$  and  $E_B = B$ .

I. Composition. Consists of two possibilities -- a union or intersection.

A. Union of A and B.

If A and B are two events in a sample space (S), the union of A and B ( $A \cup B$ ) contains all sample points in event A or B or both.

B. Intersection of A and B.

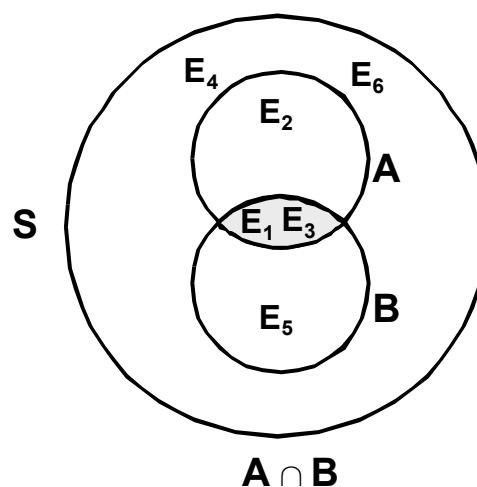
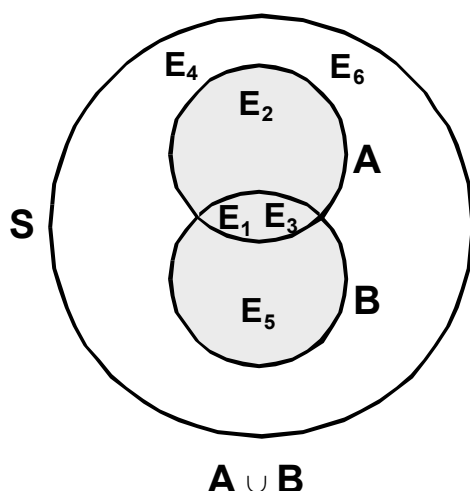
If A and B are two events in a sample space (S), the intersection of A and B ( $A \cap B$ ) is composed of all sample points that are in both A and B.



VII. MEASURE - PROBABILITY & STATISTICS  
PROBABILITY AND STATISTICS / BASIC CONCEPTS

III.B.2

## Compound Events (Continued)



### Venn Diagrams Illustrating Union and Intersection

## II. Event Relationships.

### A. Complement of an Event.

The complement of an event A is all sample points in the sample space (S), but not in A. The complement of A is  $1 - P_A$ .

### B. Conditional Probabilities.

The conditional probability of event A, given that B has occurred, is:

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \quad \text{if } P(B) \neq 0$$



VII. MEASURE - PROBABILITY & STATISTICS  
PROBABILITY AND STATISTICS / BASIC CONCEPTS

III.B.2

## Compound Events (Continued)

Event A and B are said to be independent if either:

$$P(A|B) = P(A) \text{ or } P(B|A) = P(B)$$

### C. Mutually Exclusive Events.

If event A contains no sample points in common with event B, then they are said to be mutually exclusive.

### D. Testing for Event Relationships.

Are A and B mutually exclusive, complementary, independent, or dependent? If A and B contain one or more sample points in common, they are not mutually exclusive. If event B does not contain all points in S that are not in A, then they are not complementary.